

Nonlinear Optics of Ultracold Atoms in an Optical Cavity

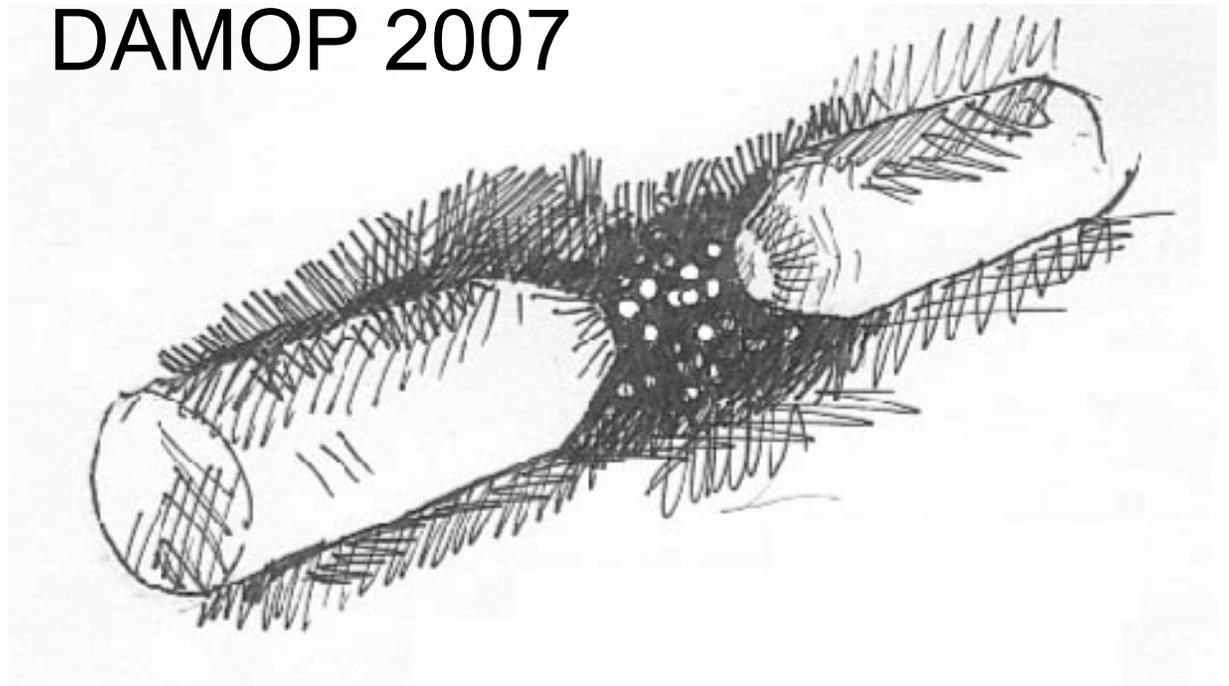
Kater Murch,

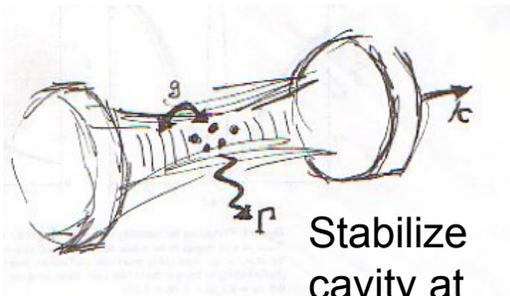
Kevin Moore, Subhadeep Gupta, Dan Stamper-Kurn
UC Berkeley

DAMOP 2007

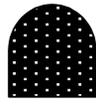
Advertisement:

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Friday: R1.00017





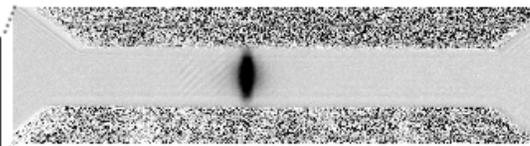
Stabilize cavity at 850nm



Detect Rb at 780nm



Top cavity mirror



Quantify transmission as the average intracavity photon number: \bar{n}

Detection efficiency:

$$\eta = 0.05$$

Cavity mirrors: Vital statistics

ROC = 5cm

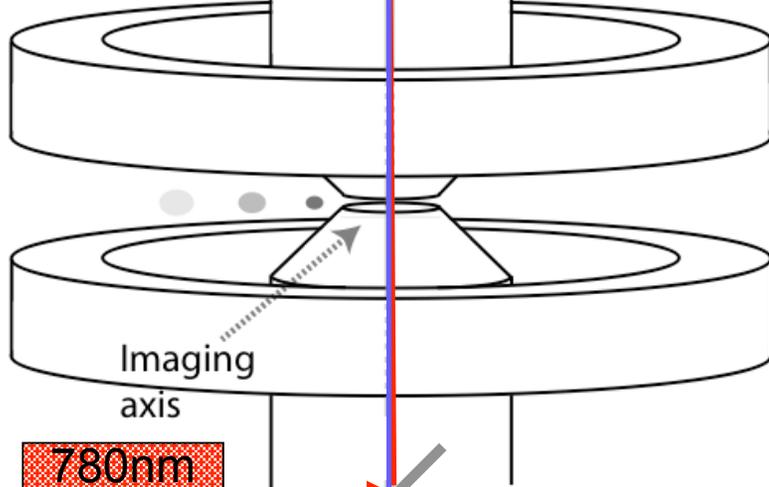
Length = 194 μm

Finesse = 584,000

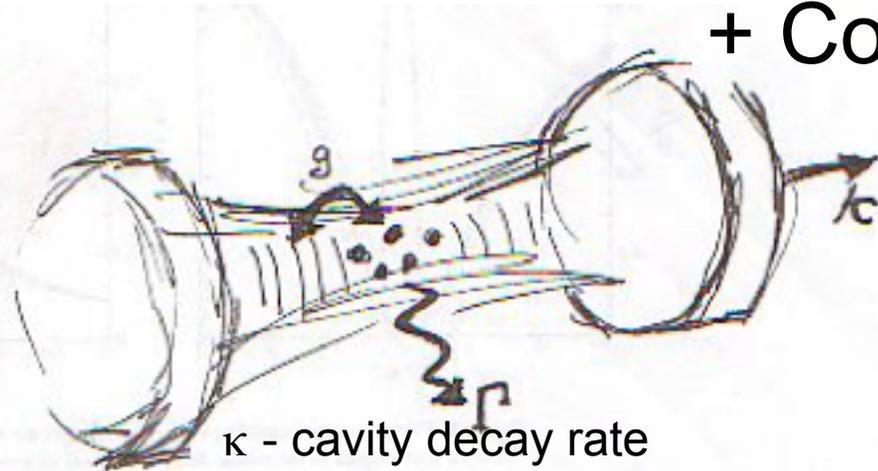
Stable ref. cavity

780nm laser

850nm laser



Cavity QED: Strong Coupling + Cold Atoms



κ - cavity decay rate

Γ - atomic decay rate

g - atom cavity coupling

Typically Nonlinear optics occurs at high intensities as conventional materials mediate weak coupling between light and matter

Strong Coupling allows access to nonlinear phenomenon at very low average photon number:

Optical bistability, cross phase modulation, photon blockade

Critical photon number

$$n_o = \gamma^2 / 2g_o^2 = .02$$

Critical atom number

$$N_o = 2\gamma\kappa / g_o^2 = .02$$

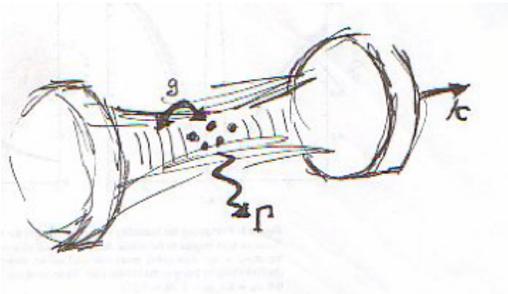
Single atom cooperativity

$$C = g_o^2 / 2\gamma\kappa = 50$$

Cold atoms introduce long lived motional coherence, hence, nonlinearities resulting from collective atomic motion may occur at very low average photon number:

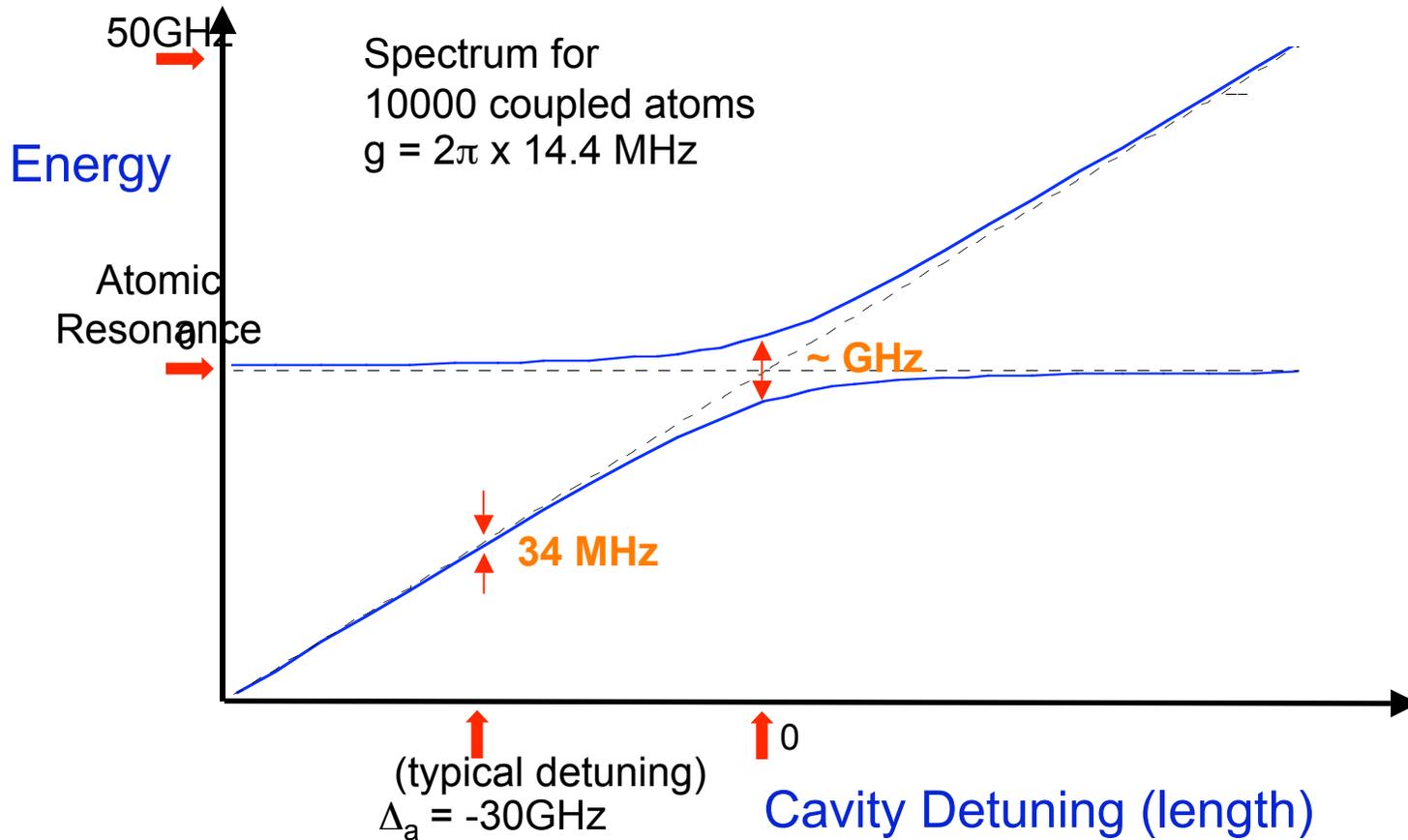
$$\bar{n} \sim \Gamma_m / \kappa$$

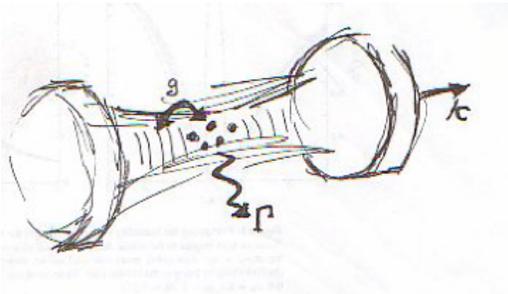
(Rempe '91, Gripp '96, Stauer '04, Turchette '95, Birnbaum '05)



Dispersive Cavity QED (far from atomic resonances)

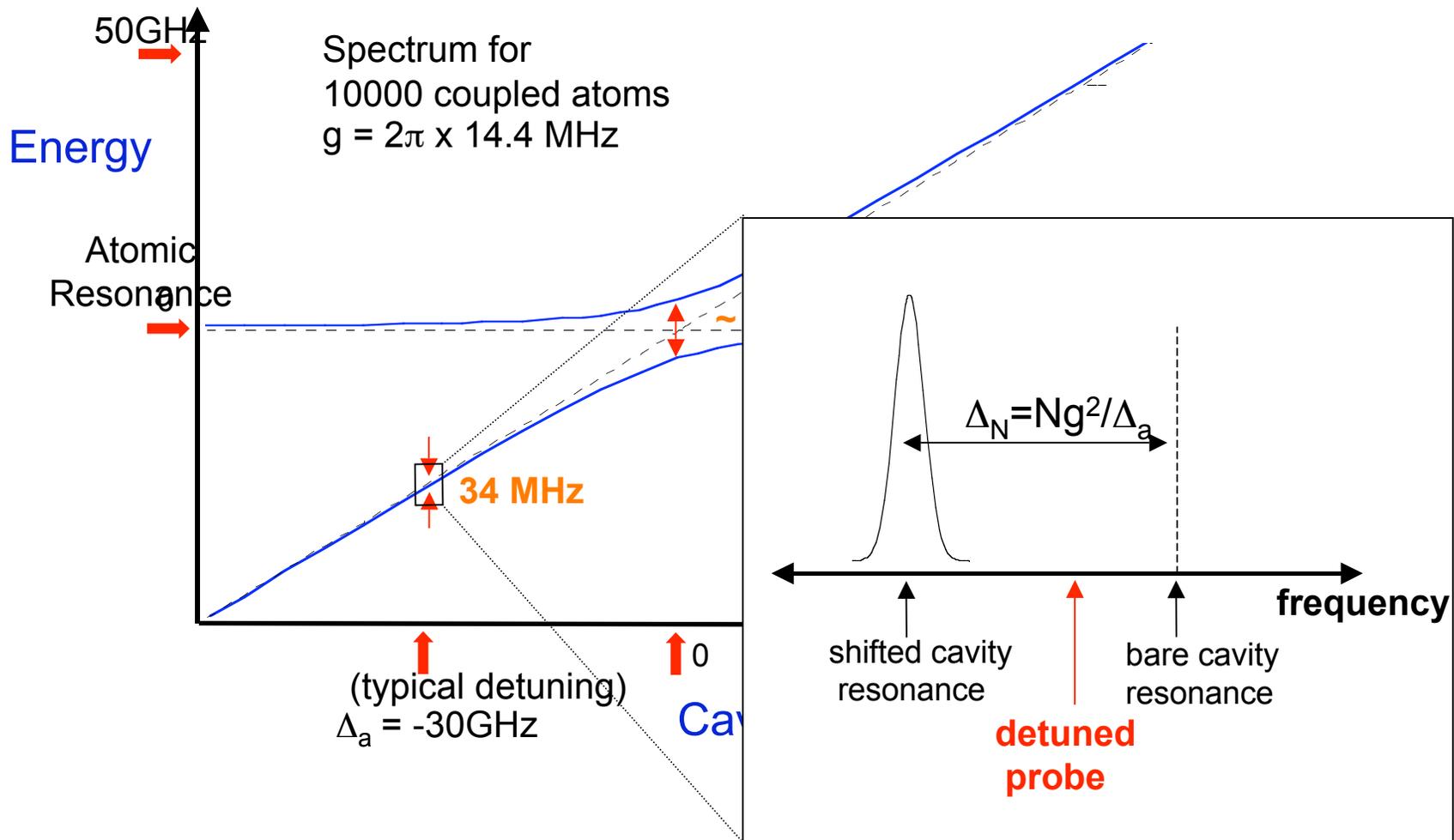
Presence of atoms basically changes the index of refraction in the cavity
 Each atom shifts the cavity resonance by an amount: g^2/Δ_a

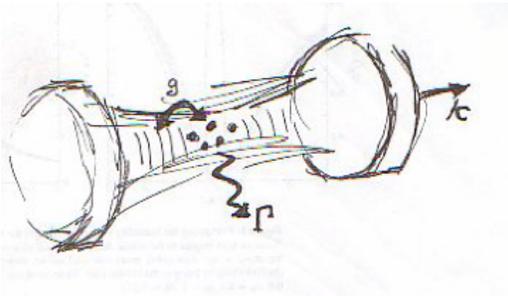




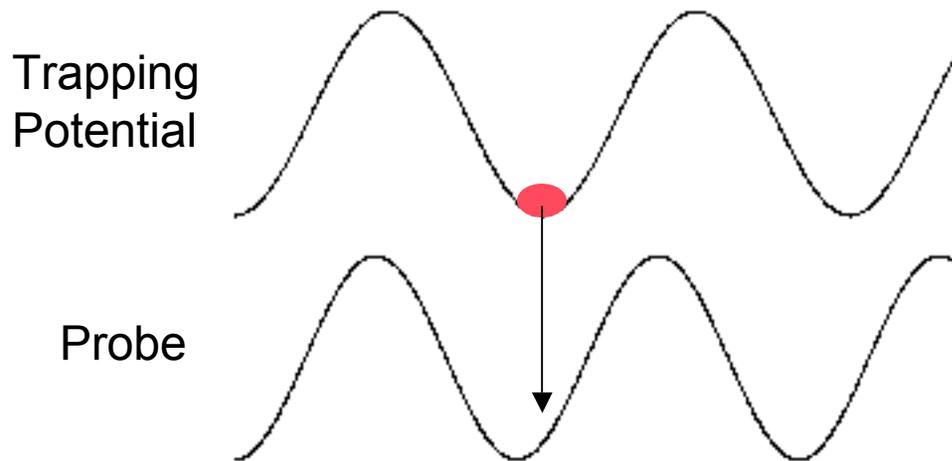
Dispersive Cavity QED (far from atomic resonances)

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Atoms occupy a 1D lattice in the cavity



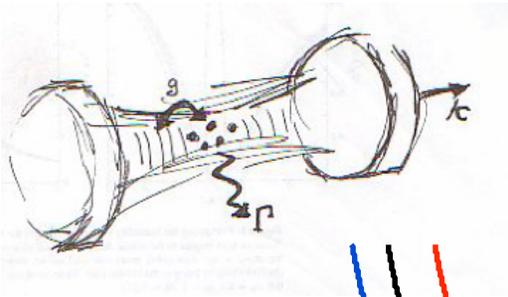
Interaction depends on intensity of the probe: this differs from well to well.

$$U(z) = U_{850}(z) + U_{780}(z,t)$$

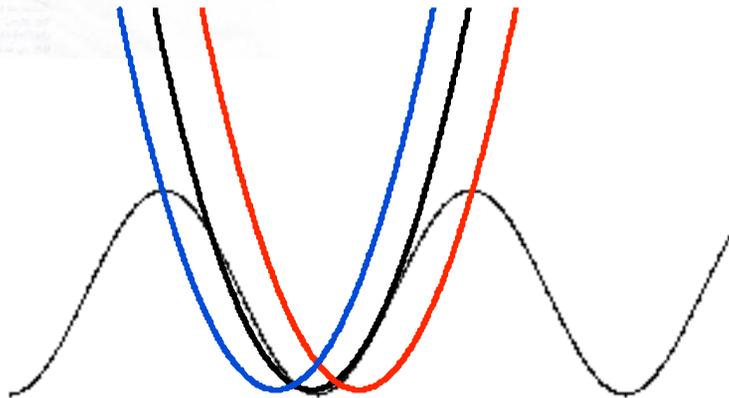
↑
Cavity is stabilized to this wavelength

↑
Varies depending on detuning from cavity resonance

$$\Delta_N = \sum_{sites} \frac{N_i g_i^2}{\Delta_a} \simeq \frac{N g_0^2}{2\Delta_A}$$



Trapping Potential



Probe



Presence of the probe shifts potential minimum.

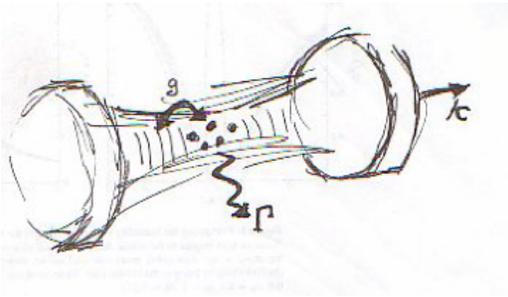
This causes the overall interaction to either **increase** or **decrease**

$$\Delta_N = N \frac{g_0^2}{2\Delta_a} \left(1 + 0.6 \frac{U_{780}}{U_{850}} \right)$$

$$U(z) = U_{850}(z) + U_{780}(z,t)$$

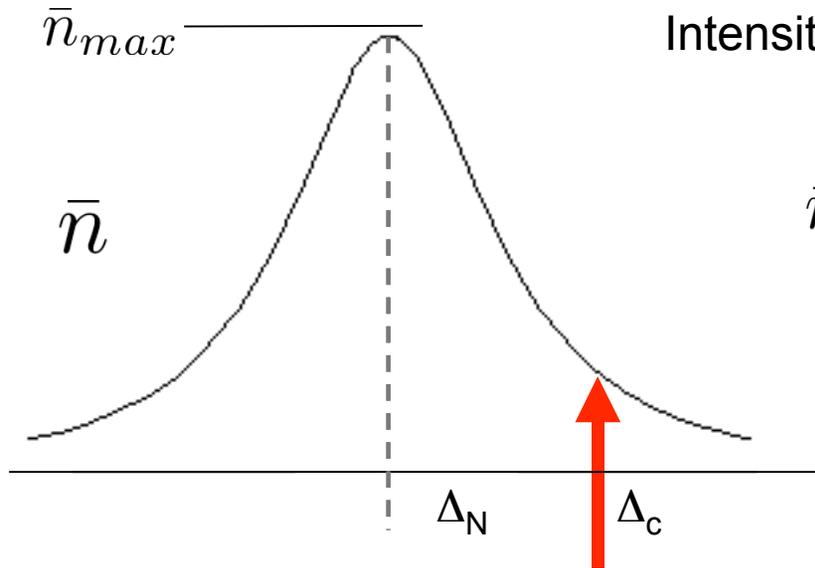
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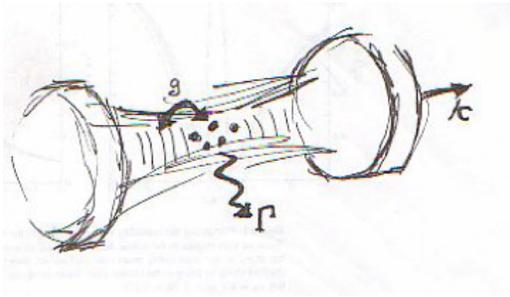


Modified cavity lineshape

Intensity in cavity is normally a lorentzian

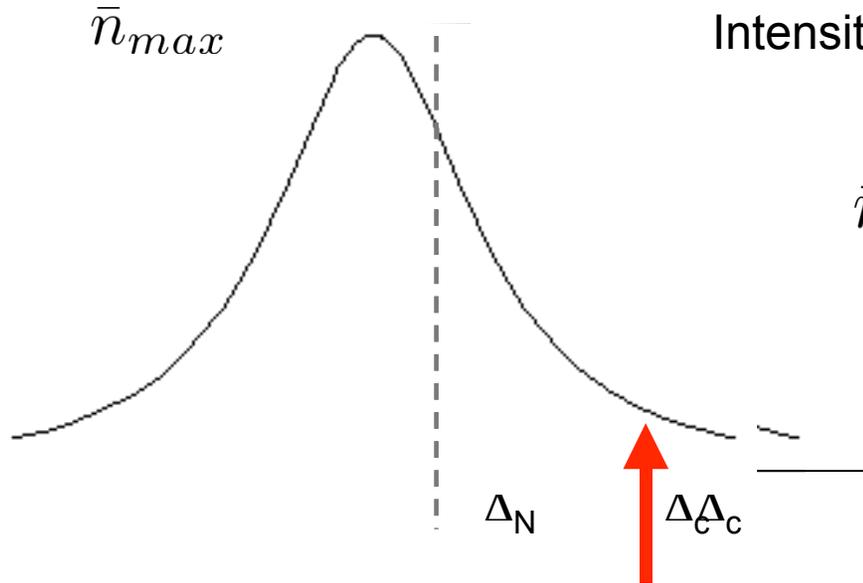


$$\bar{n} = \frac{\bar{n}_{max}}{1 + \left(\frac{\Delta_c - \Delta_N}{\kappa}\right)^2}$$



Modified cavity lineshape

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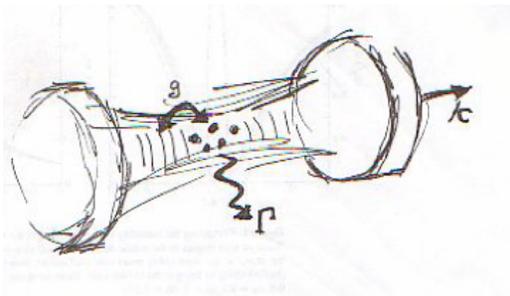
But now, Δ_N depends on the intensity,

$$\bar{n} = \frac{\bar{n}_{max}}{1 + \left(\frac{\Delta_c - \Delta_N(1 + \epsilon \bar{n})}{\kappa}\right)^2}$$

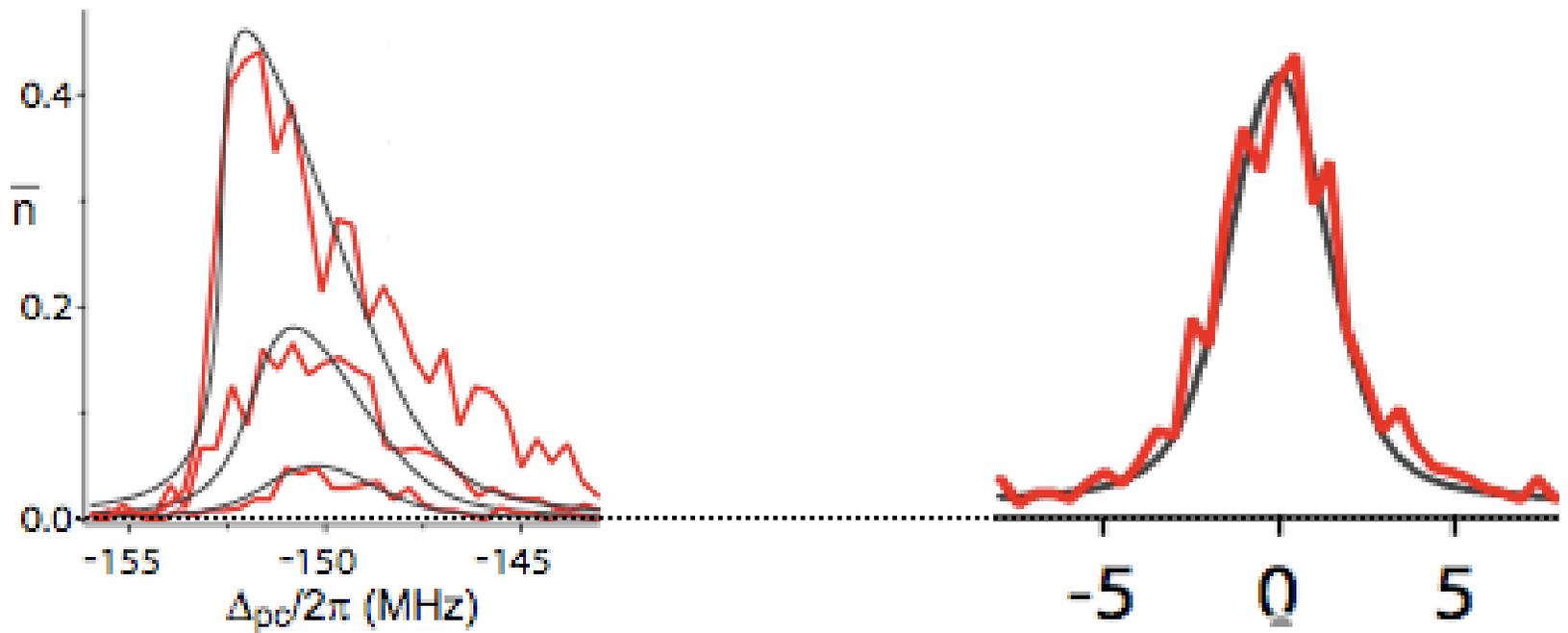
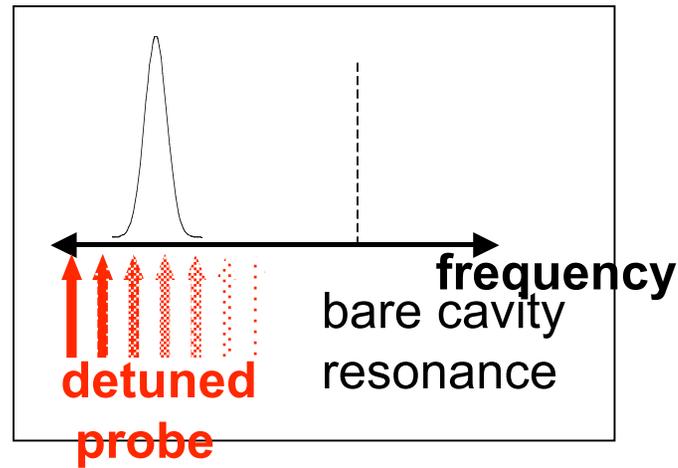
Index of refraction

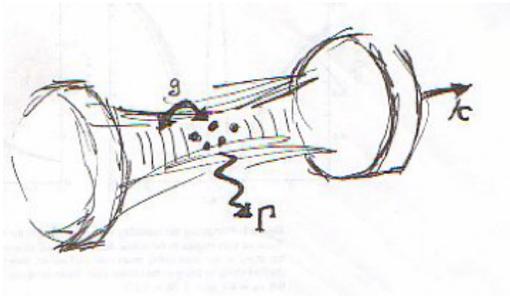
$$1 + \frac{N \langle g^2 \rangle}{\Delta_a \omega_p} = \left(1 + \frac{N g_0^2}{2 \Delta_a \omega_p}\right) + \frac{N g_0^2}{2 \Delta_a \omega_p} 0.6 U_p / U_t$$

Kerr Effect

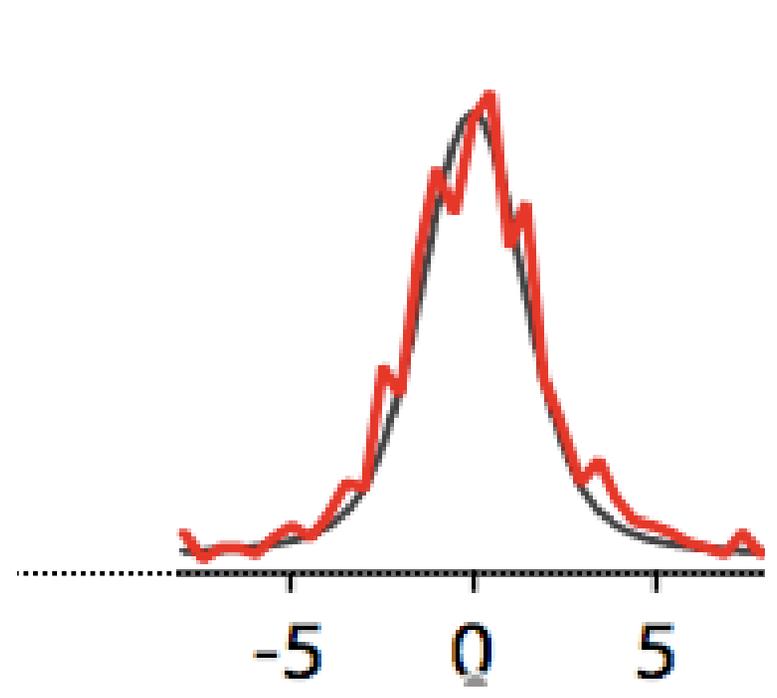
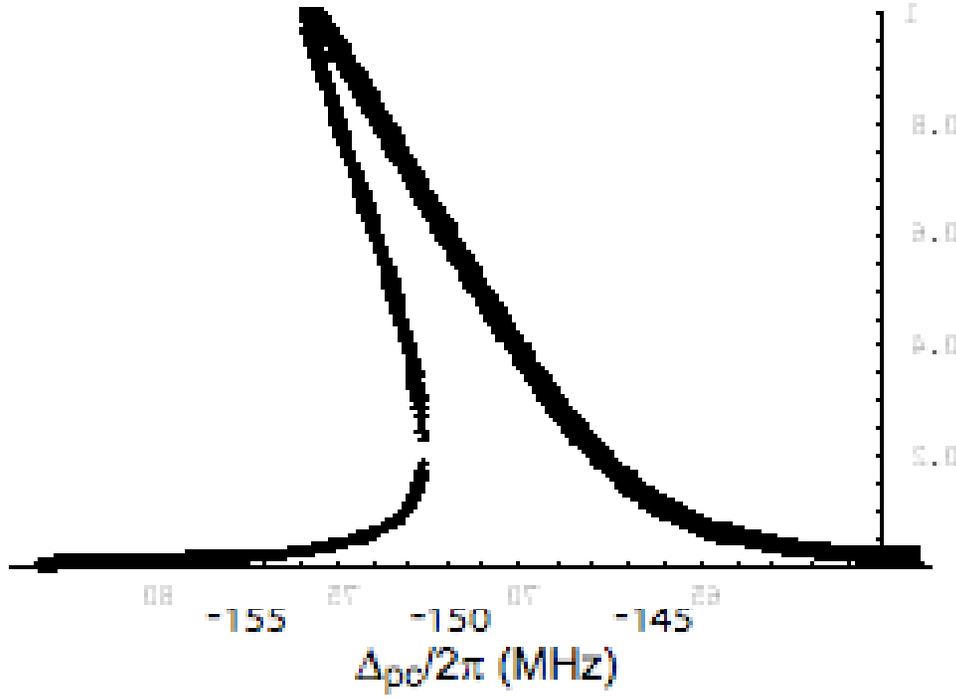
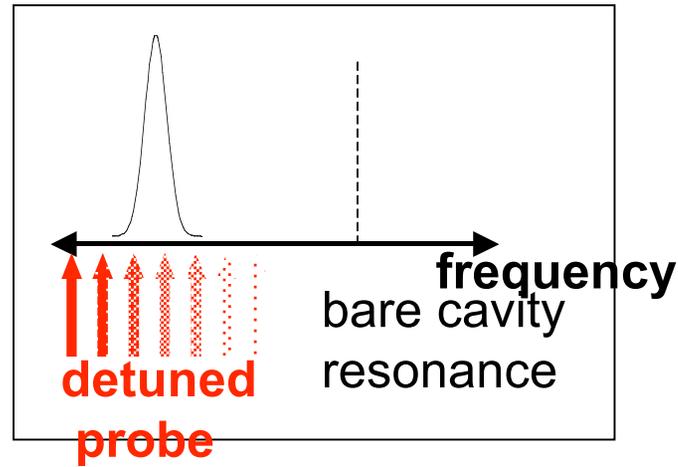


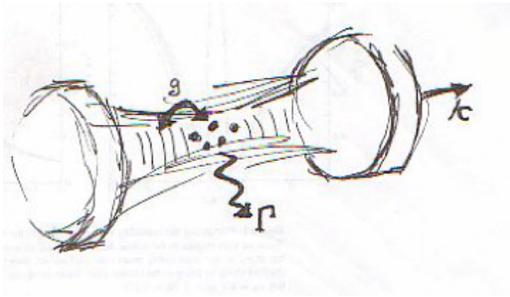
Asymmetric Line Shapes from Kerr Non-Linearity



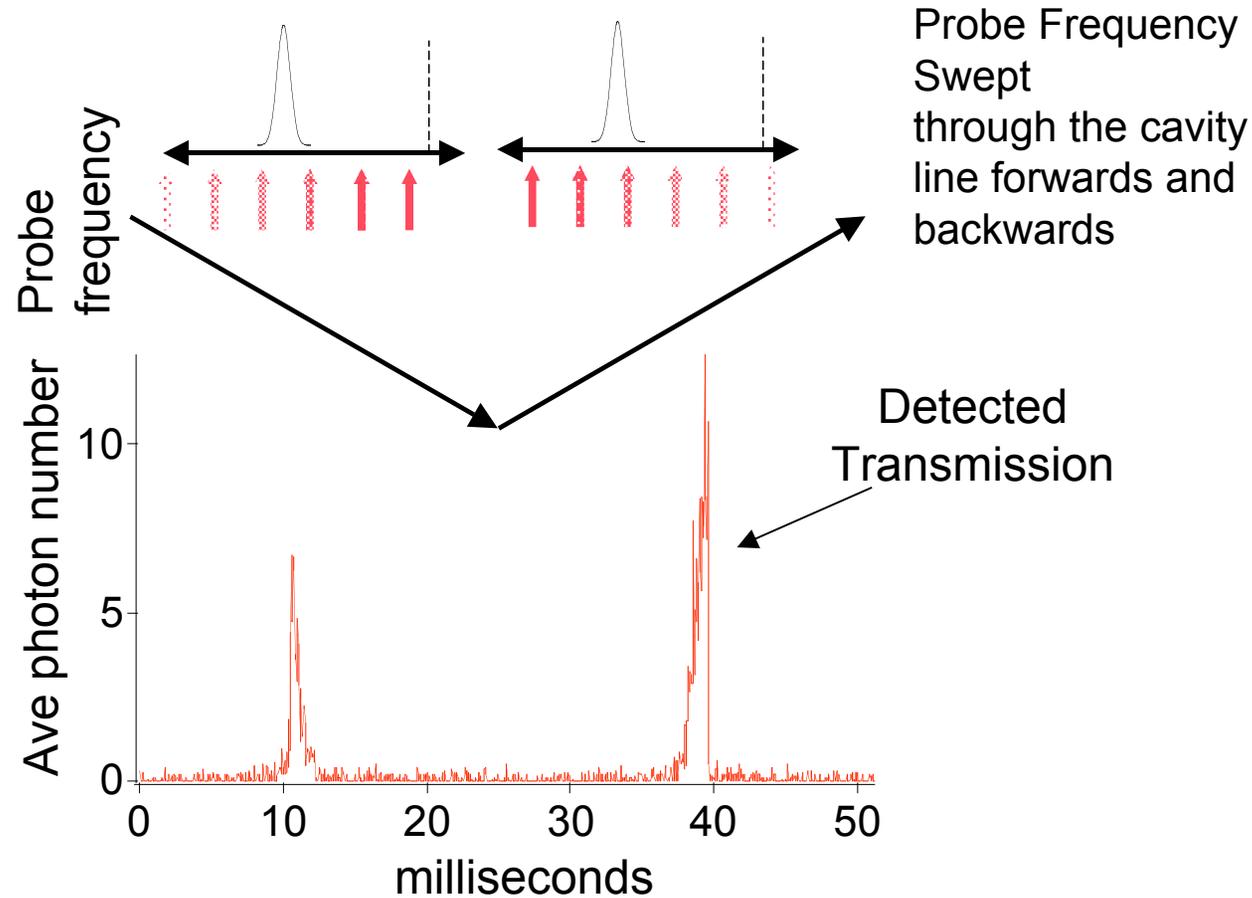


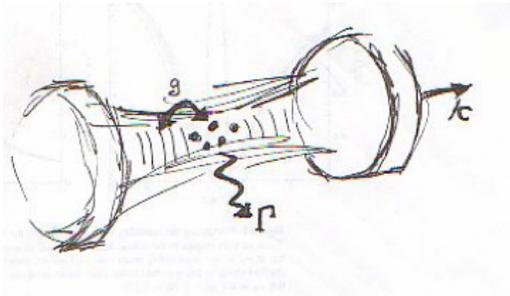
Asymmetric Line Shapes from Kerr Non-Linearity



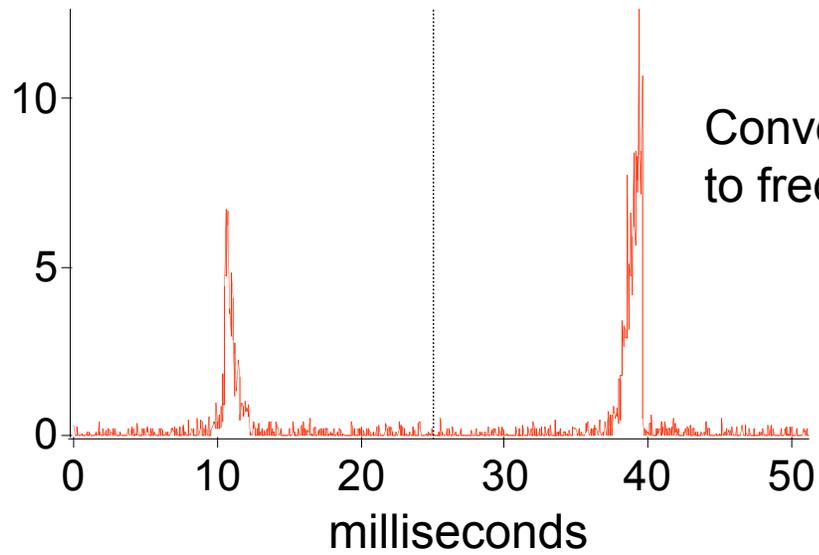


Dispersive/Refractive bistability

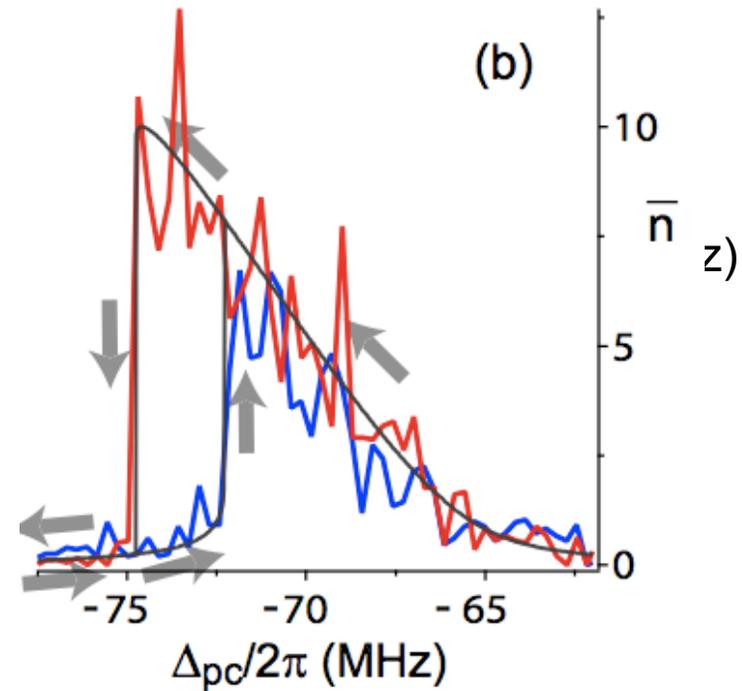
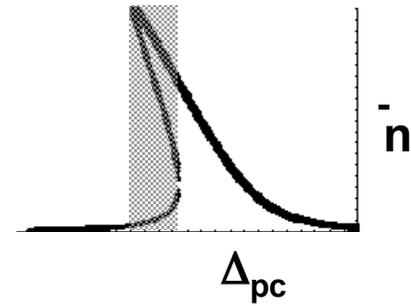


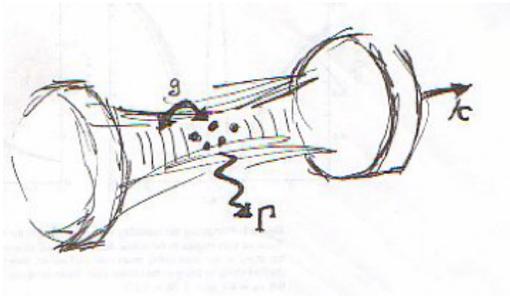


Dispersive/Refractive bistability

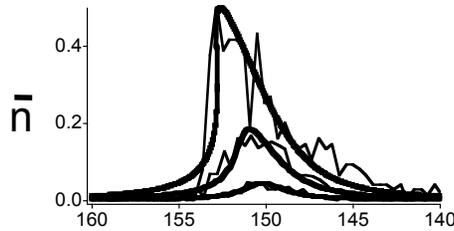


Convert
to frequency units



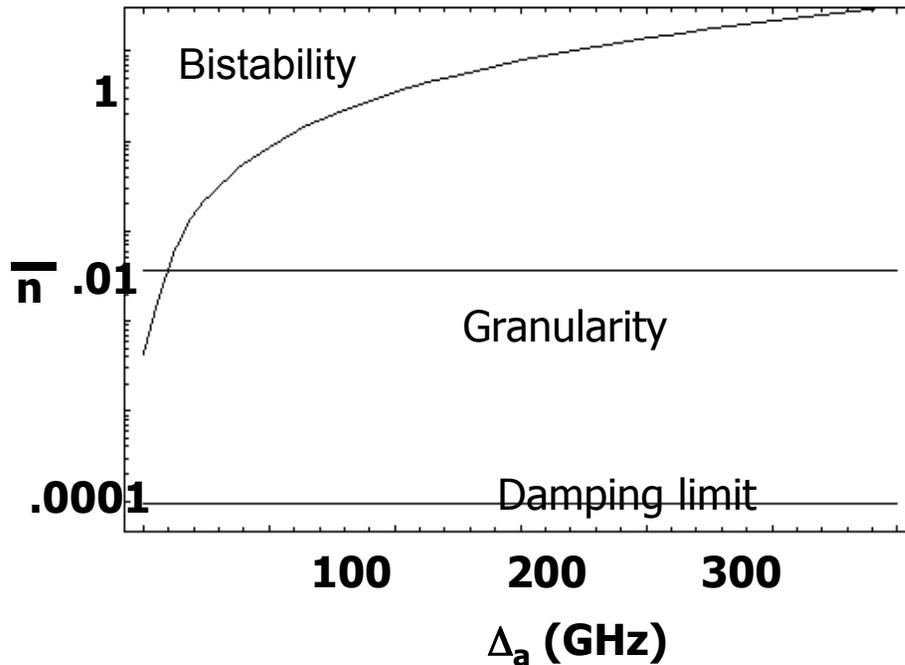


Non-linearity at very low photon numbers



As we reduce the atomic detuning, fewer photons will suffice for bistability; nonlinearities at very low photon number are obtainable.

Nonlinearity “phase diagram”



When photons arrive less frequently than the period of harmonic motion, granularity of individual photons becomes important.

Ultimately, the damping of atomic motion forces a technical limit on the nonlinearity.



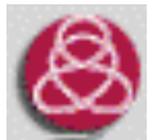
Alfred P. Sloan
Foundation

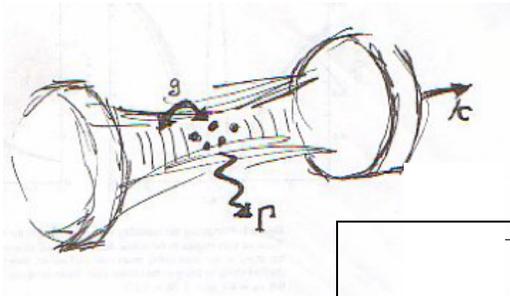


The David and Lucile Packard
Foundation

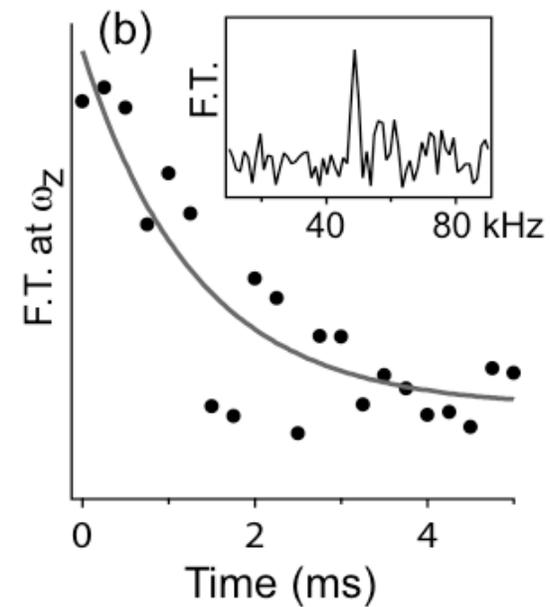
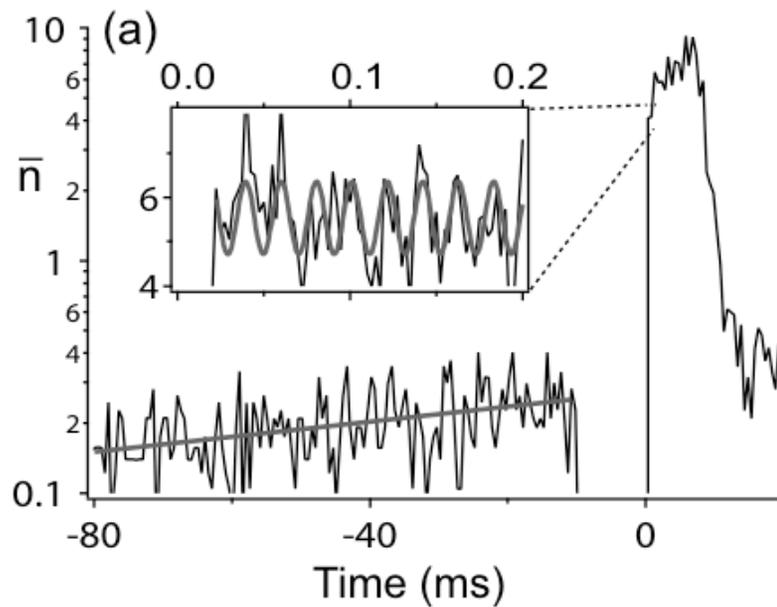
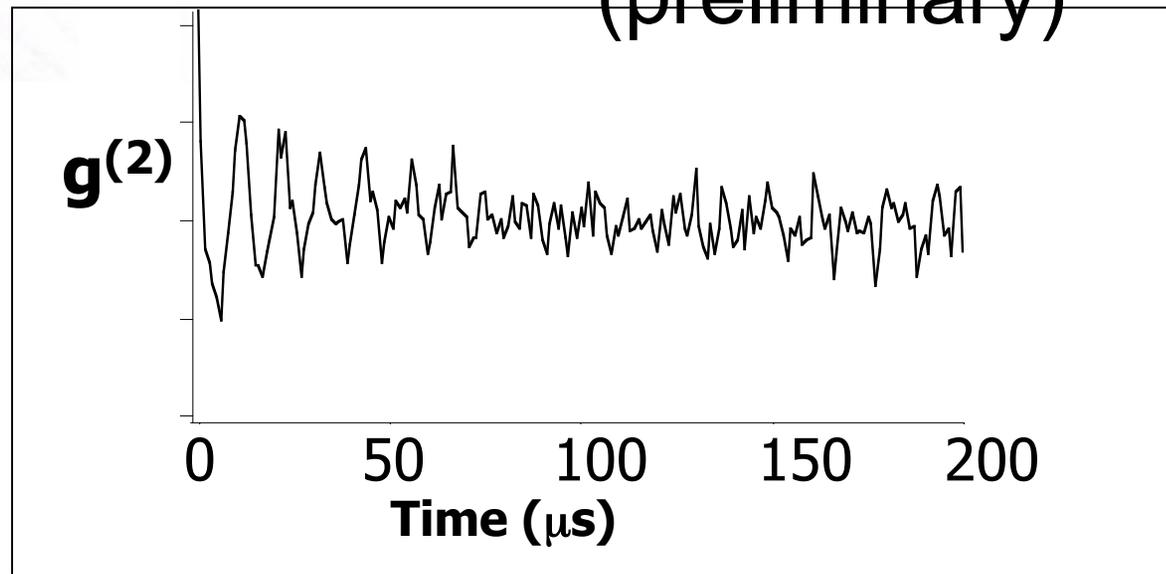


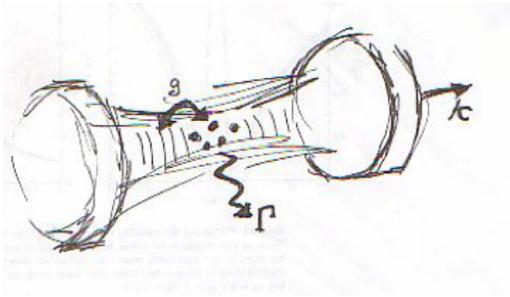
Miller
Institute



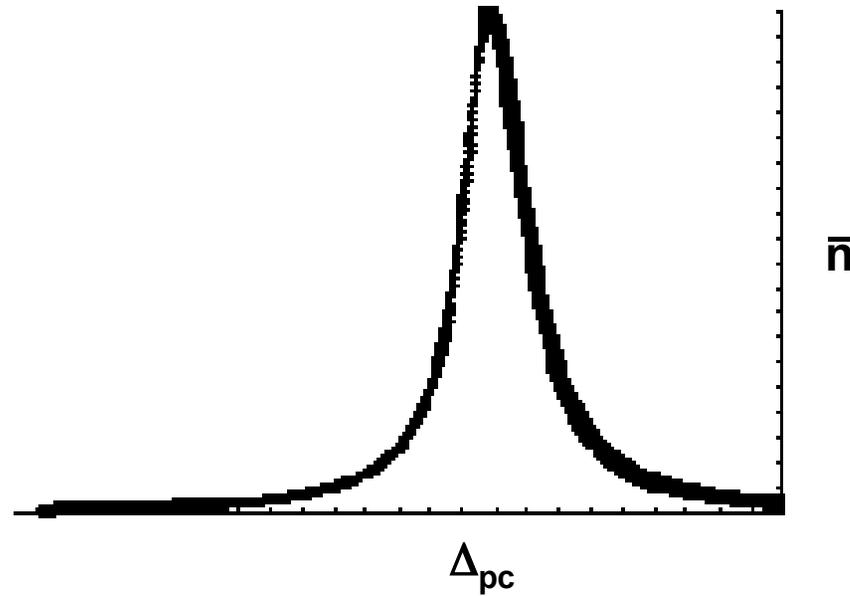


Photon correlations (preliminary)

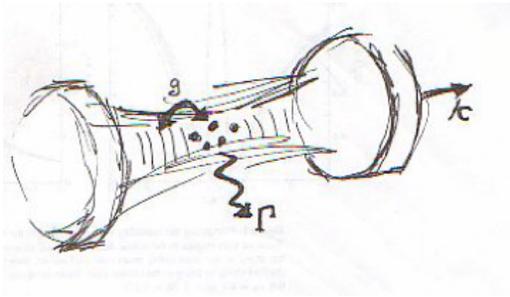




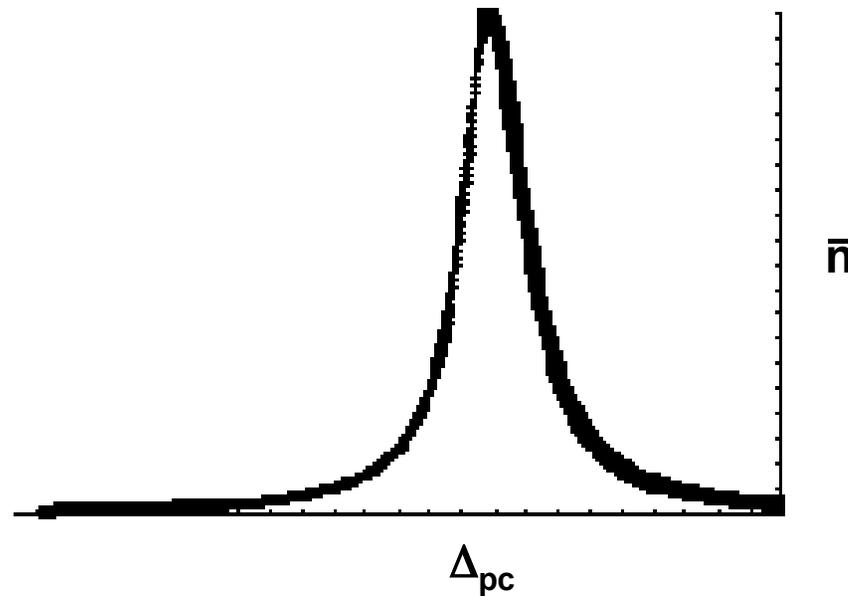
Varying the Kerr parameter



Kerr Parameter = 0.25

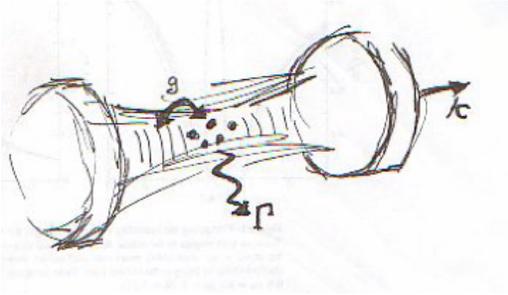


Varying the Kerr parameter

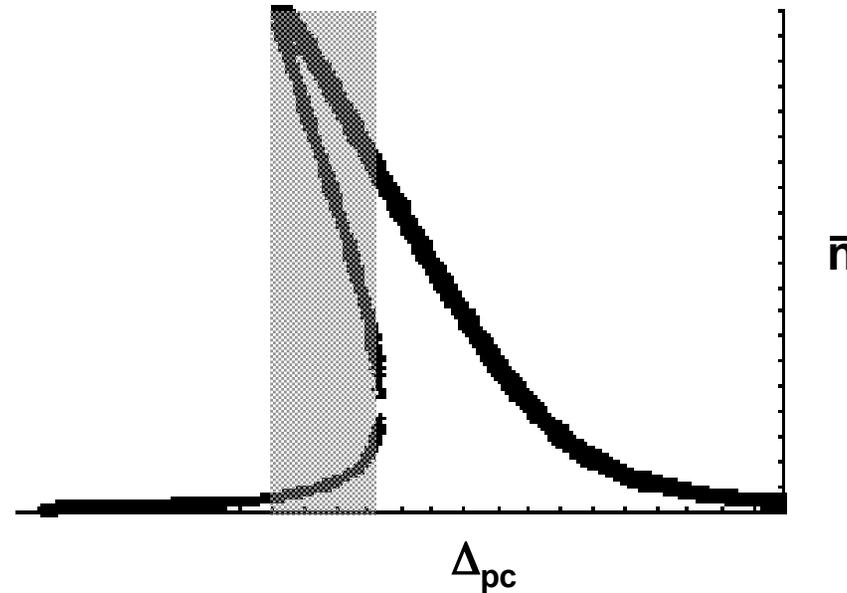


Kerr Parameter varied from
0.25 to 9.75

Strength of Nonlinearity
controlled by Δ_a or atom
number



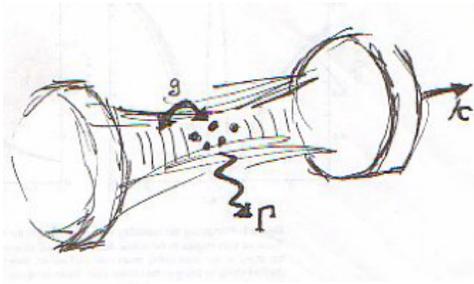
Varying the Kerr parameter



Three solutions to the cubic

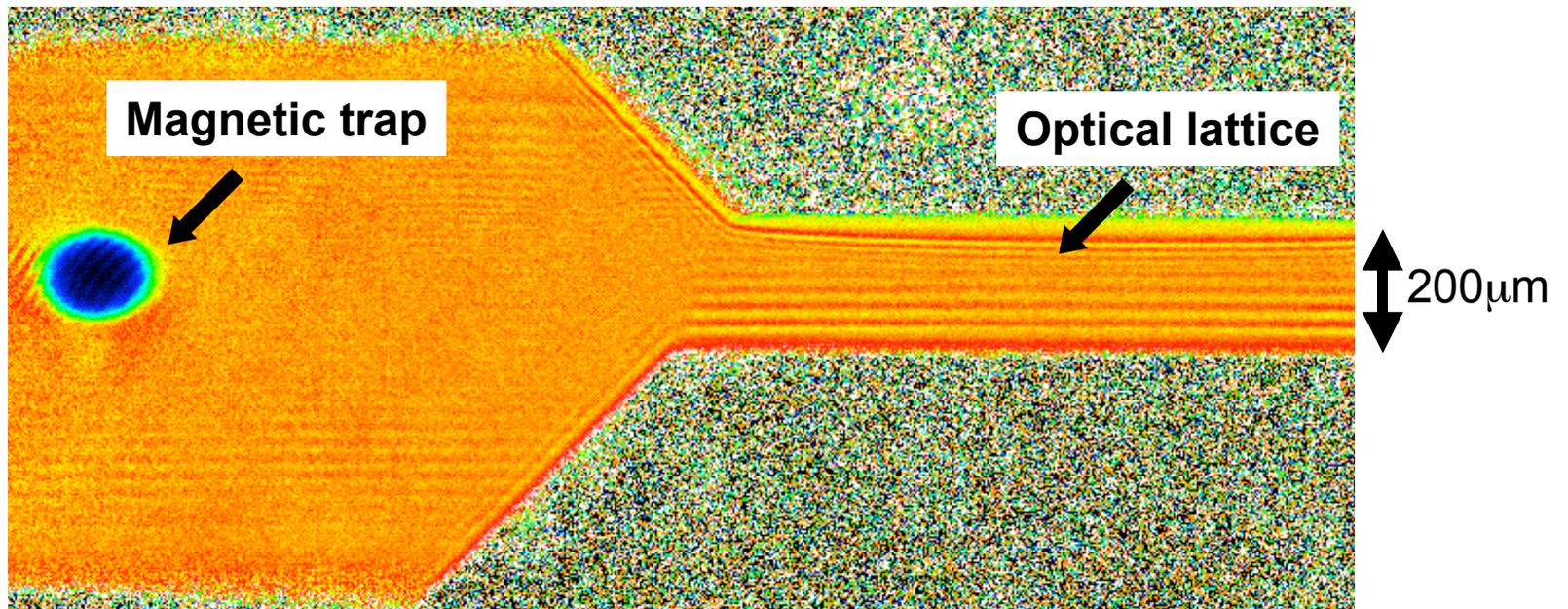
$$\bar{n} = \frac{\bar{n}_{max}}{1 + \left(\frac{\Delta_c - \Delta_N (1 + \epsilon(\bar{n}/\bar{n}_{max}))}{\kappa} \right)^2}$$

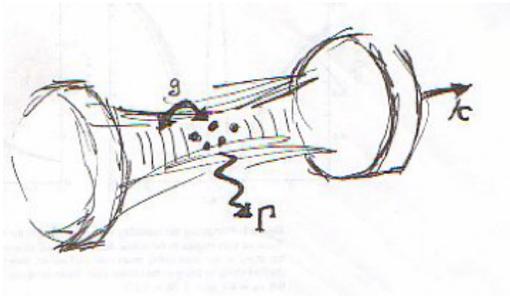
Kerr Parameter = 9.75
“Hysteresis”



Far Off-Resonant optical Trap

Cavity stabilization laser at 851nm
forms an optical dipole trap





Cold atoms integrated with high finesse cavity

